

1 A circle has radius 18 cm.

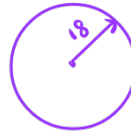
Work out the circumference of the circle.

Give your answer correct to 3 significant figures.

$$\text{circumference} = 2\pi r$$

$$= 2 \times \pi \times 18 \quad (1)$$

$$= 113 \text{ (3 s.f.)} \quad (1)$$



113

..... cm

(Total for Question 1 is 2 marks)

- 2 The diagram shows a shaded shape $ABCD$ made from a semicircle ABC and a right-angled triangle ACD .

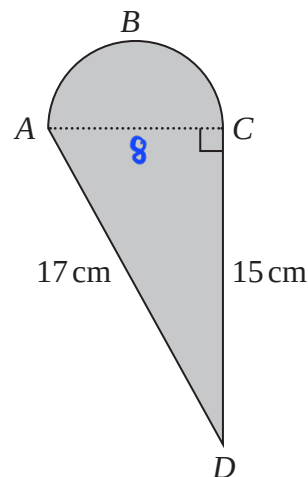


Diagram NOT
accurately drawn

AC is the diameter of the semicircle ABC .

Work out the perimeter of the shaded shape.
Give your answer correct to 3 significant figures.

By using Pythagoras' Theorem :

$$\begin{aligned} AC^2 &= AD^2 - CD^2 \\ AC^2 &= 17^2 - 15^2 \quad (1) \\ AC &= \sqrt{64} \\ &= 8 \text{ cm} \quad (1) \end{aligned}$$

$$\text{Length } ABC = \frac{\pi \times 8}{2} = 4\pi \quad (1)$$

$$\begin{aligned} \text{Perimeter of shaded shape} &: 4\pi + 15 + 17 \quad (1) \\ &= 44.6 \text{ cm} \quad (1) \end{aligned}$$

44.6

..... cm

(Total for Question 2 is 5 marks)

3 A circle has diameter 18 cm.

Work out the area of the circle.

Give your answer correct to 3 significant figures.

$$\text{Area of circle} : \pi \times r^2$$

$$= \pi \times \left(\frac{18}{2}\right)^2 \text{ (1)}$$

$$= \pi \times 9^2$$

$$= 254 \text{ (1)}$$

$$\dots\dots\dots 254 \dots\dots\dots \text{cm}^2$$

(Total for Question 3 is 2 marks)

- 4 The region, shown shaded in the diagram, is a path.

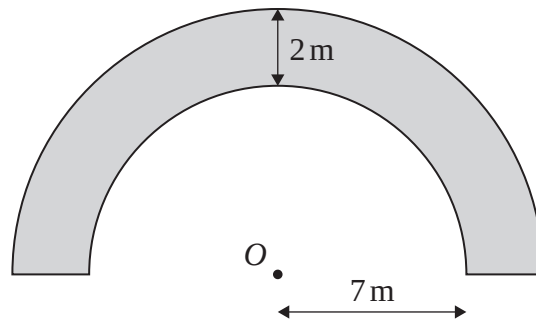


Diagram **NOT**
accurately drawn

The boundary of the path is formed by two semicircles, with the same centre O , and two straight lines.

The inner semicircle has a radius of 7 metres.

The path has a width of 2 metres.

Work out the perimeter of the path.

Give your answer correct to one decimal place.

$$\text{Inner semicircle} = \frac{1}{2} \times 2\pi r$$

$$= \pi(7)$$

$$= 7\pi \quad \textcircled{1}$$

$$\text{Outer semicircle} = \frac{1}{2} \times 2\pi r$$

$$= \pi(9)$$

$$= 9\pi$$

$$\text{Perimeter} = 9\pi + 7\pi + 2(2) \quad \textcircled{1}$$

$$= 16\pi + 4$$

$$= 54.3 \text{ (1dp)}$$

①
 54.3 m

(Total for Question 4 is 3 marks)

5 A , B and C are points on a circle with centre O .

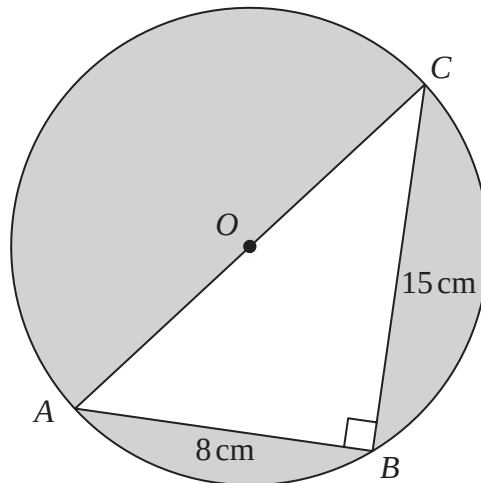


Diagram **NOT**
accurately drawn

AOC is a diameter of the circle.

$AB = 8\text{ cm}$ $BC = 15\text{ cm}$

Angle $ABC = 90^\circ$

Work out the total area of the regions shown shaded in the diagram.
Give your answer correct to 3 significant figures.

$$\text{Area of triangle} = \frac{1}{2} ab \sin C$$

$$\begin{aligned} \text{Area of triangle} &= \frac{1}{2} \times 8 \times 15 \times \sin 90^\circ \\ &= 60 \end{aligned}$$

$$\begin{aligned} AC &= \sqrt{8^2 + 15^2} \quad (1) \\ &= 17 \quad (1) \end{aligned}$$

$$\text{radius of circle} = 17 \div 2 = 8.5\text{ cm}$$

$$\begin{aligned} \text{Area of circle} &= \pi r^2 \\ &= \pi (8.5)^2 \\ &= 226.98 \quad (1) \end{aligned}$$

$$\begin{aligned} \text{Area of shaded region} &= 226.98 - 60 \quad (1) \\ &= 166.98 \\ &= 167 \text{ (3sf)} \quad (1) \end{aligned}$$

167

..... cm²

(Total for Question 5 is 5 marks)

- 6 The diagram shows a shape made from a square $ABCD$ and 4 identical semicircles.

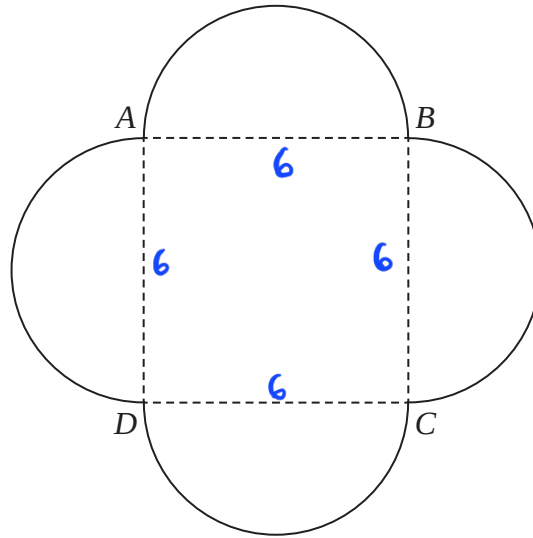


Diagram NOT
accurately drawn

As shown in the diagram, the semicircles have AB , BC , CD and DA as diameters.

The area of the square is 36 cm^2

Calculate the total area of the shape.
Give your answer correct to one decimal place.

Finding length of sides of $ABCD$:

$$x^2 = 36$$

$$x = 6 \text{ cm} \text{ (1)}$$

$\therefore$ length of side of square = diameter of semicircle = 6 cm

Area of each semicircle:

$$\frac{1}{2} \times \pi \times \left(\frac{6}{2}\right)^2 = \frac{9}{2} \pi \text{ (1)}$$

$$\begin{aligned} \text{Area of 4 semicircle : } & 4 \times \frac{9}{2} \pi \\ & = 18 \pi \end{aligned}$$

Total area: area of square + area of 4 semicircle

$$= 36 + 18 \pi \text{ (1)}$$

$$= 92.5 \text{ cm}^2 \text{ (1)}$$

92.5 cm^2

(Total for Question 6 is 4 marks)

- 7 A circle has radius 6.5 cm.

Calculate the circumference of the circle.

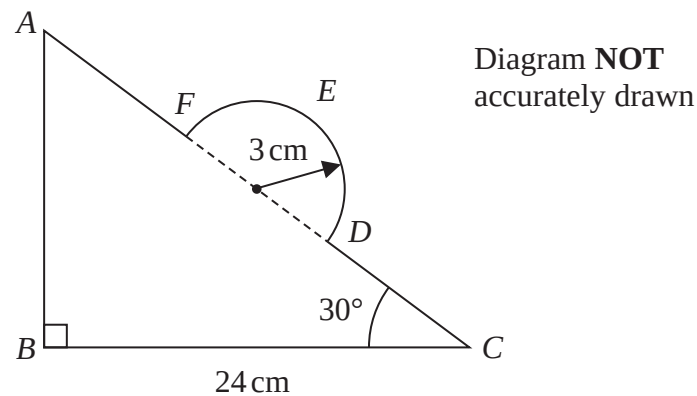
Give your answer correct to 3 significant figures.

$$\begin{aligned}\text{circumference} &= 2 \times \pi \times 6.5 \quad (1) \\ &= 40.8 \quad (1)\end{aligned}$$

40.8 cm

(Total for Question 7 is 2 marks)

8 In the diagram, ABC is a right-angled triangle and DEF is a semicircular arc.



In triangle ABC

$$BC = 24 \text{ cm}$$

$$\text{angle } ABC = 90^\circ$$

$$\text{angle } BCA = 30^\circ$$

The points D and F lie on AC so that DF is the diameter of the semicircular arc DEF .
The radius of the semicircular arc is 3 cm.

Work out the length of $AFEDC$

Give your answer correct to 2 significant figures.

$$\cos 30^\circ = \frac{24}{AC} \quad (1)$$

$$AC = \frac{24}{\cos 30^\circ} = 27.712 \dots \quad (1)$$

$$FED = \frac{1}{2} \times 2 \times \pi \times 3 \quad (1)$$

$$= 3\pi = 9.424 \dots$$

$$AFEDC = 27.712 - 3 - 3 + 9.424 \quad (1)$$

$$= 31 \quad (1)$$

31

..... cm

(Total for Question 8 is 5 marks)

9 R and T are points on a circle, centre O

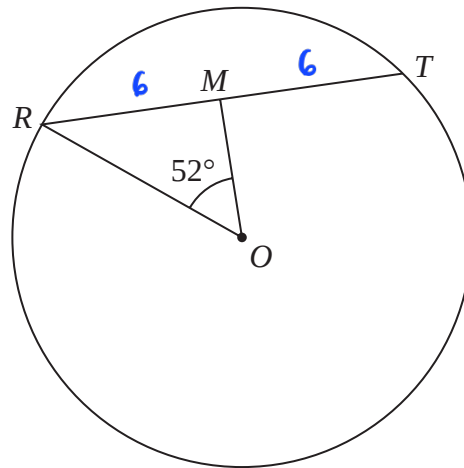


Diagram **NOT**
accurately drawn

$$RT = 12 \text{ cm}$$

M is the midpoint of RT

$$\text{Angle } ROM = 52^\circ$$

Work out the area of the circle.

Give your answer correct to 3 significant figures.

$$\sin 52^\circ = \frac{6}{r} \quad (1)$$

$$r = \frac{6}{\sin 52^\circ} \quad (1)$$

$$\approx 7.614$$

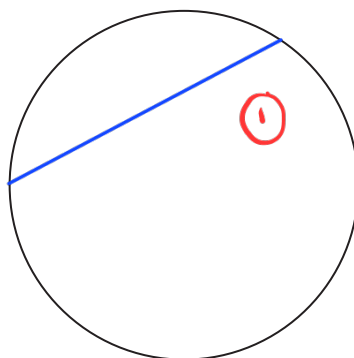
$$\text{Area} = \pi \times 7.614^2 \quad (1)$$

$$\approx 182 \quad (1)$$

182

..... cm^2

(Total for Question 9 is 4 marks)



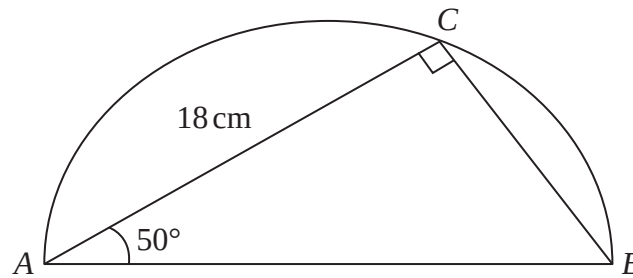
10 (c) On the diagram above, draw a chord of the circle.

(1)

(Total for Question 10 is 1 marks)

11 The diagram shows a triangle ABC inside a semicircle.

Diagram **NOT**
accurately drawn



A , B and C are points on the semicircle.

AB is the diameter of the semicircle.

Angle $ACB = 90^\circ$

Angle $BAC = 50^\circ$

$AC = 18 \text{ cm}$

Work out the perimeter of the semicircle.

Give your answer correct to 2 significant figures.

$$\cos 50^\circ = \frac{18}{AB} \quad (1)$$

$$AB = \frac{18}{\cos 50^\circ} \quad (1)$$

$$= 28.0030 \dots$$

$$\frac{1}{2} \times \pi \times 28.0030 \dots = 43.9 \dots \quad (1)$$

$$28.0030 \dots + 43.9 \dots \quad (1)$$

$$= 71.9900 \dots$$

$$\approx 72 \quad (1)$$

72

..... cm

(Total for Question 11 is 5 marks)

12 A circle has radius 8.5 cm

Work out the circumference of the circle.

Give your answer correct to 3 significant figures.

$$\text{circumference} = 2 \times \pi \times 8.5 \quad \textcircled{1}$$

$$= 53.4 \quad \textcircled{1}$$

53.4

..... cm

(Total for Question 12 is 2 marks)